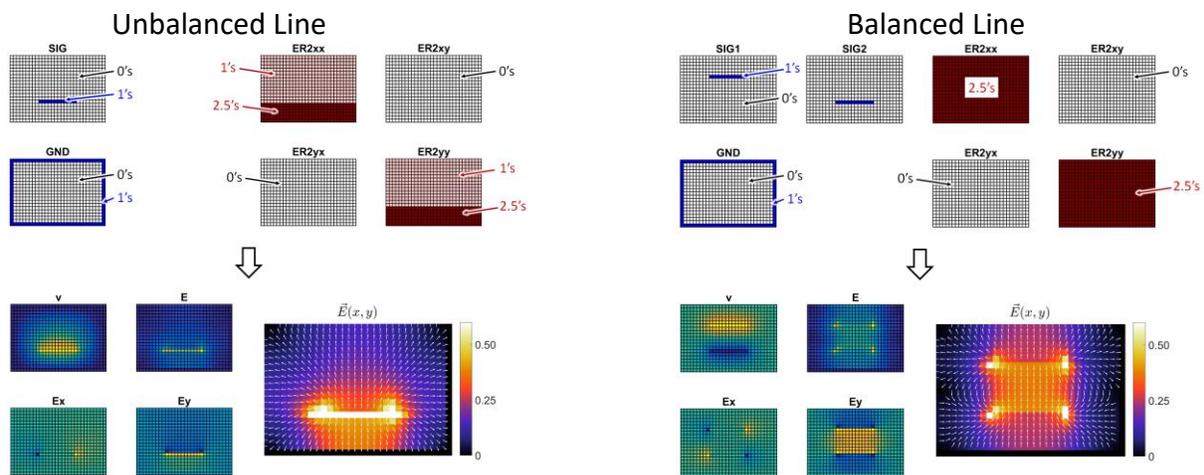


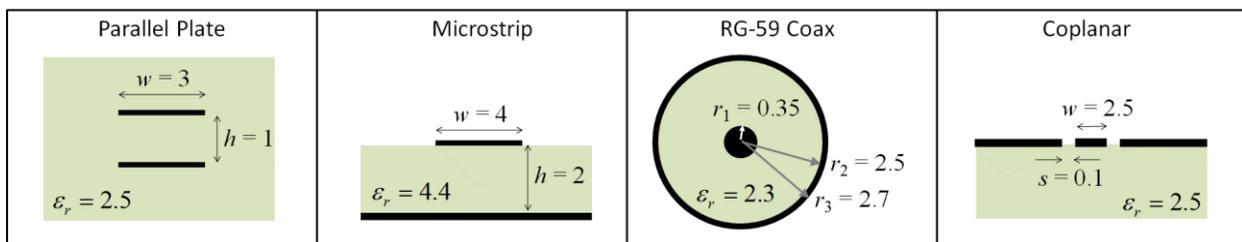
Problem #1: Generic Transmission Line Simulator

Write a generic MATLAB program to simulate an arbitrary transmission line embedded in a fully anisotropic medium. The program shall construct four arrays ER_{xx} , ER_{xy} , ER_{yx} , and ER_{yy} defining the elements of the permittivity tensor. In addition, the program shall construct three arrays $SIG1$, $SIG2$, and GND to describe balanced transmission lines and two arrays SIG and GND to describe unbalanced lines. The program should calculate the electric potential $V(x, y)$ (volts), electric field intensity $\vec{E}(x, y)$ (V/m), distributed capacitance C (F/m), distributed inductance L (H/m), characteristic impedance Z_c (ohms), and effective refractive index n_{eff} . The input and output functions for an ordinary microstrip (unbalanced transmission line) and an ordinary parallel plate (balanced transmission line) are shown below where $\epsilon_r = 2.5$.



Problem #2: Benchmark Simulations

For each transmission line shown below, calculate the transmission line parameters (i.e. L , C , Z_0 , and n_{eff}) and plot the electric potential $V(x, y)$ and electric field $\vec{E}(x, y)$. Use the `quiver()` command to superimpose the vector information onto the field magnitude as shown in the figures above.



Notes: The parallel plate and coplanar transmission lines incorporate ABS plastic which has a relative permittivity of 2.5. This is a material commonly used in 3D printing. The substrate of the microstrip transmission line is FR-4 which has a relative permittivity of 4.4. The RG-59 coax is the standard coaxial cable for television prior to HDMI. The dielectric is Teflon which has a relative permittivity of 2.3.

Problem #3: Spatially Variant Anisotropic Media

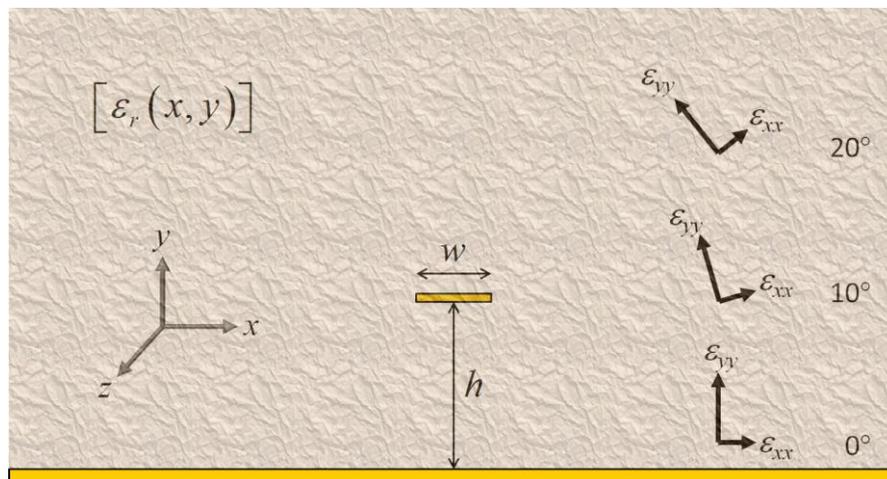
A microstrip transmission line with $w = 4$ and $h = 3$ is to be completely embedded within a spatially variant anisotropic medium (SVAM) with the following dielectric tensor. The material possesses negligible magnetic response so $\mu_r = 1.0$.

$$[\epsilon_r] = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 9 & 0 \\ 0 & 0 & 6 \end{bmatrix}$$

The orientation of the tensor is rotated about the z -axis by $\phi = 10^\circ$ for every distance h above the substrate. This is done in a smooth and continuous manner so that the tensor rotation as a function of height above the substrate is

$$\phi(y) = \frac{y}{h}(10^\circ).$$

If you do this correctly, $\phi = 0^\circ$ at the ground plane, $\phi = 5^\circ$ at $h/2$ above the ground plane, $\phi = 10^\circ$ at the signal conductor, and $\phi = 20^\circ$ at a distance $2h$ above the ground plane. This is illustrated in the figure below.



Plot the nine tensor functions, conductors, scalar potential, and the electric field.

Provide the transmission line parameters L , C , Z_0 , and n_{eff} .

Discuss your results and make meaningful conclusions.