



SIGN CONVENTIONS FOR EM WAVES

EE 3321 Electromagnetic Field Theory

Pioneering 21st Century
Electromagnetics and Photonics



<http://emlab.utep.edu>

EQUATION(S)	ELECTRICAL ENGINEERING (Negative Sign Convention)	PHYSICS / SCIENCE (Positive Sign Convention)
Wave Propagating in +z Direction	$\cos(\omega t \mp kz)$ – forward wave $\exp(\mp jkz)$ + backward wave	$\cos(-\omega t \pm kz)$ – backward wave $\exp(\pm ikz)$ + forward wave
Maxwell's Equations	$\nabla \times \vec{E} = -j\omega\vec{B}$ $\nabla \cdot \vec{D} = \rho_v$ $\nabla \times \vec{H} = \vec{J} + j\omega\vec{D}$ $\nabla \cdot \vec{B} = 0$ $\vec{D} = \epsilon\vec{E}$ $\vec{B} = \mu\vec{H}$	$\nabla \times \vec{E} = i\omega\vec{B}$ $\nabla \cdot \vec{D} = \rho_v$ $\nabla \times \vec{H} = -\vec{J} - i\omega\vec{D}$ $\nabla \cdot \vec{B} = 0$ $\vec{D} = \epsilon\vec{E}$ $\vec{B} = \mu\vec{H}$
Wave Vector	$k = \beta - j\alpha$	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> $\alpha < 0$ gain (grow) $\alpha > 0$ loss (decay) </div> <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;"> $\beta < 0$ backward $\beta > 0$ forward </div> $k = \beta + i\alpha$
Refractive Index	$\tilde{n} = n - j\kappa$	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> $n < 0$ negative index $n > 0$ positive index </div> <div style="border: 1px solid black; padding: 5px; display: inline-block; margin-left: 20px;"> $\kappa < 0$ gain (growth) $\kappa > 0$ loss (decay) </div> $\tilde{n} = n + i\kappa$
Lorentz Model	$\tilde{\epsilon}_r(\omega) = 1 + \frac{\omega_p^2}{\omega_0^2 - \omega^2 + j\omega\Gamma}$	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> $\Gamma < 0$ gain (grow) $\Gamma > 0$ loss (decay) </div> $\tilde{\epsilon}_r(\omega) = 1 + \frac{\omega_p^2}{\omega_0^2 - \omega^2 - i\omega\Gamma}$

$$-j \leftrightarrow i$$

$$\alpha < 0 \text{ gain (grow)}$$

$$\alpha > 0 \text{ loss (decay)}$$

$$\beta < 0 \text{ backward}$$

$$\beta > 0 \text{ forward}$$

$$n < 0 \text{ negative index}$$

$$n > 0 \text{ positive index}$$

$$\kappa < 0 \text{ gain (growth)}$$

$$\kappa > 0 \text{ loss (decay)}$$

$$\Gamma < 0 \text{ gain (grow)}$$

$$\Gamma > 0 \text{ loss (decay)}$$